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# A generalized electric model for mono and polycrystalline silicon in the presence of cracks and random defects

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## Abstract

Damage, micro-cracks, grain boundaries and other defects in solar cells are impacting on the electric power-loss of photovoltaic modules, their actual solar conversion efficiency and also their lifetime. In the present contribution, a one-dimensional model for simulating the electric current distribution in solar cells accounting for a distributed series resistance is generalized to the presence of partially conductive cracks. The proposed model is used to perform a quantitative analysis of electroluminescence (EL) images of cracked monocrystalline silicon solar cells. A further generalization in a stochastic direction is also proposed in order to take into account randomly distributed defects typical of polycrystalline silicon.

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**Keywords:** electric model; cracks; distributed defects; monocrystalline silicon; polycrystalline silicon, electroluminescence.

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## 1. Introduction

Cracking in Silicon solar cells is an important factor for the electrical power-loss of photovoltaic modules. Cracks on the millimeter or centimeter size, mostly invisible by naked eye, can lead to electrically inactive cell areas, thus reducing the power output of the module and the fill factor [1]. This takes place via the following mechanisms, i.e: a linear decreasing of the short circuit current by increasing the inactive cell area [2-4], and an increase in the series resistance of the cell due to cracking [2,5]. For instance, experimental results [5] have shown an increase in the

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series resistance of the cell of about 7% due to cracking with a corresponding power-loss of 4% and a fill factor reduction of 3%. Other experimental investigations [2] have shown that cracks inserted in solar cells by the application of a uniform pressure to simulate snow can lead up to 1.5% of power loss. After the subsequent application of 200 humidity freeze cycles according to standard specifications [6], such cracks propagate, the electrically disconnected areas increase in size and up to 10% of power loss has been reported. Potentially, if a crack crossing a conductor (called finger) is sufficiently open, then the finger may fail and the electric flow to the busbar in case of normal operating condition, or from the busbar in case of forward bias condition as in the EL testing, would be interrupted. Therefore, portions of Si cells can be potentially deactivated by cracks and their impact on power-loss reasonably depends on their inclination and position with respect to the busbars, see Figs. 1(a) and (b). For instance, a crack parallel to the busbar on the upper side of the cell could lead up to 25% of electrically inactive area (Fig. 1(b)). According to this pure geometrical criterion which does not take into account neither physical mechanisms such as thermo-mechanical deformation, nor the fact that the cells are embedded in the composite PV module, worst-case scenarios have been predicted by considering all the experimentally detected [2] or numerically simulated [7] cracks as perfectly insulated lines. In reality, it is reasonable to expect intermediate configurations where cracks may partially conduct depending on the relative crack opening displacement at crack faces [8].

At present, electric models of solar cells do not consider this form of coupling induced by cracking. Usually, a discretization of the solar cell is made in the plane and a one-diode or a two-diodes models are applied to each node of the mesh to predict the electric response of the semiconductor [9,10]. In such approaches, the series resistance applied to each node is an equivalent one taking into account all different resistances (emitter, contact, metallization). However, it is independent on the position of the node with respect to the fingers and busbars grid. Recently, a one-dimensional model has been proposed taking into account the contribution of the grid conductivity to the distributed series resistance [11]. Nevertheless, so far, cracks and defects are never taken into account. In the present contribution, the one-dimensional model for current distribution is improved to consider the presence of cracks crossing the fingers grid. This is done by introducing a localized series resistance at the crack due to a partial opening of the crack faces. Also, the presence of randomly distributed defects is taken into account in a statistical sense, allowing a direct extension of the model to polycrystalline Si cells.

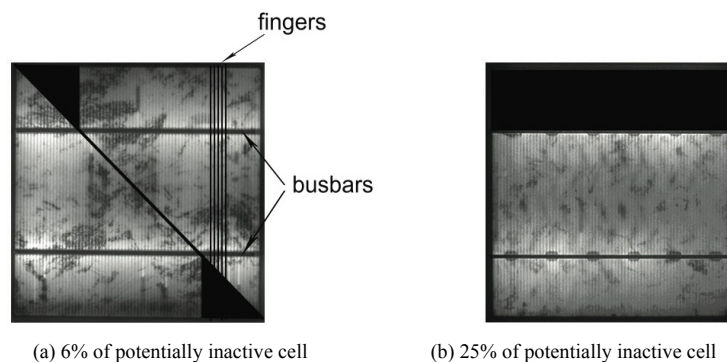


Fig. 1. Geometrical criterion showing the expected amount of potentially inactive cell areas depending on the orientation of the crack with respect to the busbars (a,b).

## 2. A one-dimensional electric model with distributed series resistance and its generalization in case of cracks

### 2.1. Electric model for undamaged monocrystalline Si cells

Recent studies have evidenced that the strongest spatial variation of the series resistance,  $R_s$ , in a Si cell is in the fingers grid direction, where the lateral series resistance is dominated by the resistance of the grid lines [11]. On the contrary, the variation of  $R_s$  from grid line to grid line due to the emitter sheet resistance is smaller, and mainly due to a shadowing effect of the fingers. Therefore, the description of the distributed  $R_s$  of the whole cell may be analyzed with a one-dimensional model focusing on the variation of the grid line resistance. In this case, the electron

current from busbar to busbar along a generic finger (see Fig. 2), is described by the following parameters: the vertical diode current density,  $I_v$ , with units of A/cm<sup>2</sup>, the horizontal current density,  $I_h$ , with units of A/cm, and the voltage,  $V$ , having units of V. All these terms vary along the  $x$  coordinate (parallel to the finger's direction, as shown in Fig. 2). Without illumination, defining  $I_h(x)$  as the horizontal current density at position  $x$  and  $I_v(x)$  the vertical diode current density in the same position, as shown in Fig. 2, for each  $x$  the following equations hold:

$$\frac{\partial V(x)}{\partial x} = V'(x) = -\rho_s I_h(x) \quad (1)$$

$$\frac{\partial I_h(x)}{\partial x} = -I_v(x) \quad (2)$$

$$\frac{\partial^2 V(x)}{\partial x^2} = V''(x) = \rho_s I_v(x) \quad (3)$$

where  $\rho_s = R_{\text{grid}} D$  is the sheet resistance in the  $x$ -direction,  $R_{\text{grid}}$  is the grid resistance ( $\Omega/\text{cm}$ ), and  $D$  is the distance between two grid lines. In the case of a low current density,  $I_v$  can be considered as constant. Therefore, Eq. (3) can be easily integrated over  $x$  and the well-known parabolic distribution is obtained for the voltage profile. On the other hand, if higher cell current values are considered, the local vertical current density is no longer a constant, and it should be computed from the following implicit equation:

$$I_v(x) = I_{01} \exp \frac{V(x) - R_{\text{loc}} I_v(x)}{n_1 V_T} - I_{\text{sc}} \quad (4)$$

where  $I_{\text{sc}}$  is the short circuit current density under illumination ( $I_{\text{sc}}=0$  in the dark case),  $R_{\text{loc}}$  is the local sheet resistance, in series with the local diode (in undamaged monocrystalline Si cells it can be assumed as a homogeneous resistance within the whole cell,  $R_{\text{hom}}$ ),  $I_{01}$  is the saturation current density,  $n_1=1$  is the ideality factor, and  $V_T=kT/e$  is the thermal voltage.

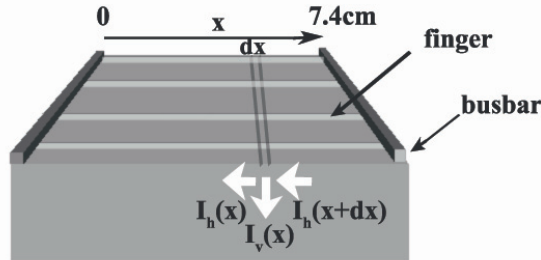


Fig. 2. Schematic representation of investigated area with  $I_v$  and  $I_h$  as the vertical and horizontal current densities, respectively.

Due to the implicit nature of Eq. (4), the voltage distribution along the grid line cannot be obtained in a closed form. On the other hand, Eq. (4) can be numerically solved using a Newton-Raphson method as proposed in [7], and Eqs. (1)-(3) can be numerically evaluated by subdividing the integration path along the grid line into equidistant intervals of length  $dx$ . The vertical current density  $I_v(x)$  is assumed constant within each interval. Under such an hypothesis, the voltage profile within the considered interval  $dx$  has still a parabolic shape, given by the following equations:

$$V(x+dx) = V(x) + V'(x)dx + \frac{V''(x)}{2}dx^2 \quad (5)$$

$$V'(x+dx) = V'(x) + V''(x)dx \quad (6)$$

In the case of undamaged monocrystalline Si cells, due to symmetry reasons, the starting point for the step-by-step integration process is the middle position between the two busbars ( $x_0=3.7$  cm with reference to the scheme in Fig. 2). Hence, the starting boundary conditions in this point are given by symmetry conditions:

$$V(x_0) = V_0; \quad V'(x_0) = 0 \quad \text{or} \quad I_h(x_0) = 0 \quad (7)$$

Starting from  $x=x_0$  and going towards one of the two busbars (a symmetric behavior is expected), the value of the vertical current density  $I_v$  is computed from Eq. (4). Then, the values of the local voltage  $V(x+dx)$  and its gradient  $V'(x+dx)$  at the end of each interval are computed from Eqs. (5) and (6), by substitution of Eqs. (1) and (3). Analogously, the increment of  $I_h$  within each interval is given by the following equation:

$$I_h(x+dx) = I_h(x) + I_v(x)dx \quad (8)$$

Note that the direction of integration is opposite to the direction of electron current (arrows in Fig. 2) and we consider dark conditions. Therefore, both  $V'$  and  $V''$  are positive. Applications of this approach to intact monocrystalline cells (no-discontinuities in the current flow along the grid line) have been proposed in [11].

## 2.2. Generalization of the electric model in case of cracks

The presence of a crack crossing a Si cell and the fingers grid determines a discontinuity in mechanical, thermal, and electric fields. In the latter case, in fact, the crack introduces an additional resistance along the current path that influences the distribution of the vertical and the horizontal current densities, as well as the voltage distribution. The value of such a resistance, in the following referred to as  $R_{cr}$ , is presumably related to the value of the crack opening displacement: the largest is the crack opening the highest is the electric resistance. The effects of a crack on the distribution of the vertical diode current density,  $I_v$ , within a cell is evident from the analysis of the EL image of a cracked cell. The brightness of the EL image, in fact, is proportional to  $I_v$  [12]. When the crack opening displacement is sufficiently large, a discontinuity in the grey-scale is evidenced on the opposite sides of the crack.

The one-dimensional electric model proposed in [11] and outlined in the previous section is herein extended to consider the presence of a crack. To this aim, a discontinuity in the voltage distribution along the grid line is introduced in correspondence of the crack,  $x_{cr}$ :

$$V(x_{cr}^+) = V(x_{cr}^-) + R_{cr}I_h(x_{cr}) \quad (9)$$

Then, the same step-by-step procedure previously outlined is applied, with some modifications in the application of the boundary conditions. In this case, in fact, symmetry conditions are no longer valid, and different considerations have to be done in order to select the starting point  $x_0$  of the integration path. In this approach, it is selected in order to obtain, as a result of the integration process, the same value of the voltage in correspondence of the two busbars. The boundary conditions defined in Eq. (7) are applied in the position  $x_0$  and the step-by-step integration procedure is applied twice, once towards the left-hand busbar and once towards the right-hand busbar. The jump in the voltage given by Eq. (9) is applied when, along the integration path, the crack is intercepted. The same approach can be pursued in case two cracks are crossing the fingers' grid. The starting point will be in the

portion between the two cracks and, therefore, a jump in the voltage will be considered along both the integration paths.

The proposed method is applied to pre-cracked monocrystalline Si cells embedded in semi-flexible modules made of 2 rows of 5 cells (see [8] for more details). Loaded and unloaded conditions have been considered in order to change the stress field in the cells. The application of a bending stress to the panel, in fact, determined an increase of the crack opening displacement of the pre-existing cracks. The distribution of the vertical diode current density,  $I_v$ , and the voltage along a selected grid line, obtained by the numerical model, is reported in Fig. 3 for a finger crossed by one crack. The parameters assumed for all the simulations are:  $I_{sc}=0$ ,  $R_{loc}=0.2 \Omega\text{cm}^2$ ,  $V_T=25 \text{ mV}$ ,  $\rho_s=0.138 \Omega$ ,  $I_{01}=1.48 \times 10^{-12} \text{ mA/cm}^2$ . The value of the other parameters, specific for each simulation, are reported in the captions of Fig. 3. The vertical current density is compared to the distribution of the EL along the same grid line, suitably rescaled by a scale factor (black dots in Figs. 3a and 3b, for unloaded and loaded condition, respectively). The numerically simulated  $I_v$  fits very well the experimental current determined from the EL data. The localized resistance due to the crack is just considered here as a free parameter as  $x_0$  and  $V_0$ , used to better fit the EL experimental data and to obtain the same voltage in correspondence of the two busbars at  $x=0$  and  $x=7.4 \text{ cm}$ . Future developments will regard the correlation between this localized resistance and the crack opening.

The same analysis has been done along a finger belonging to the same Si cell but crossed by two cracks, see Fig. 4. Again, an excellent matching with experimental data is shown.

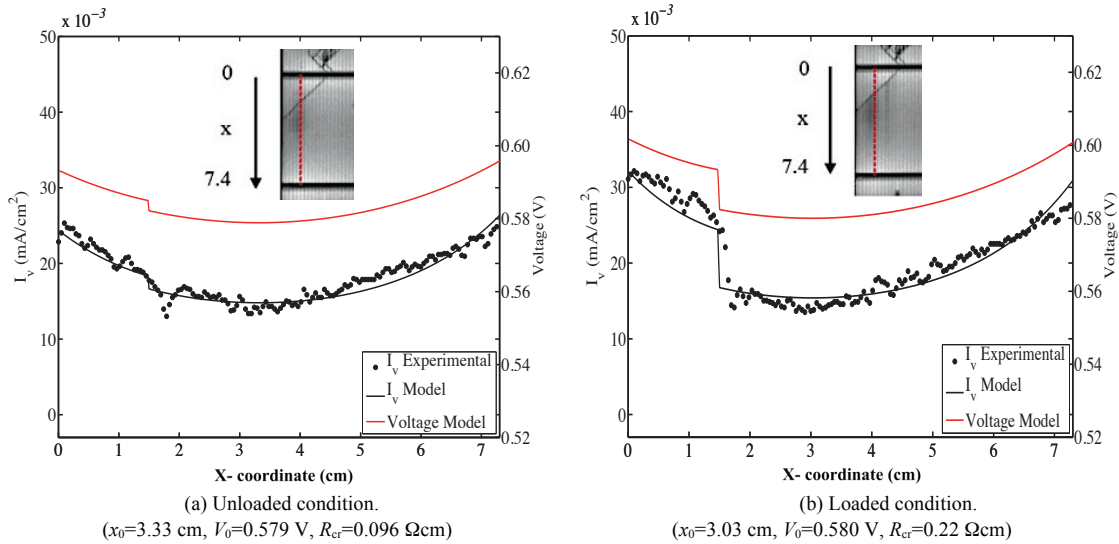


Fig. 3. Vertical current and voltage in a monocrystalline Si cell along a finger crossed by one crack: (a) unloaded and (b) loaded conditions.

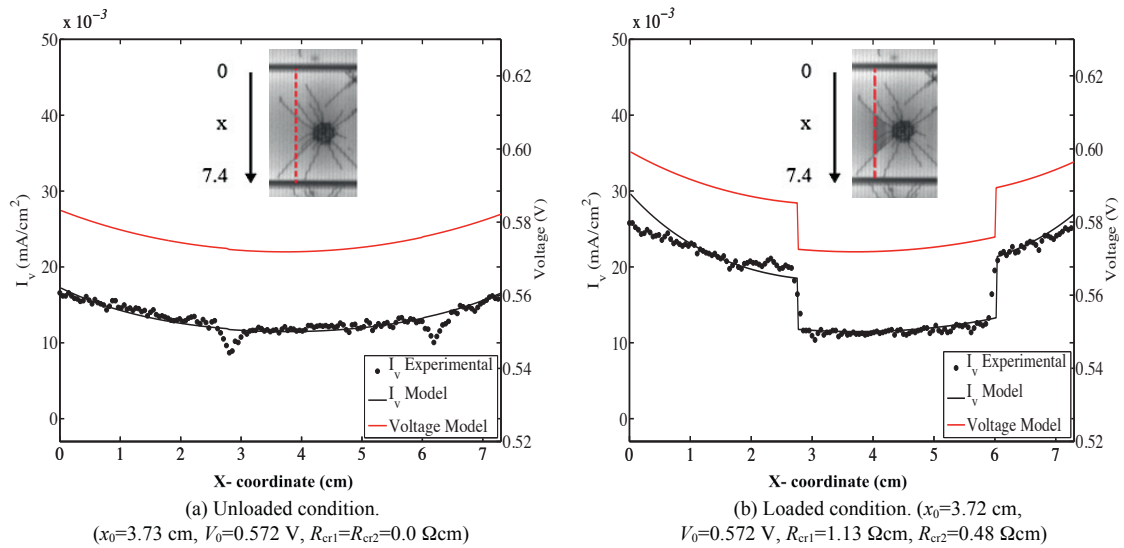
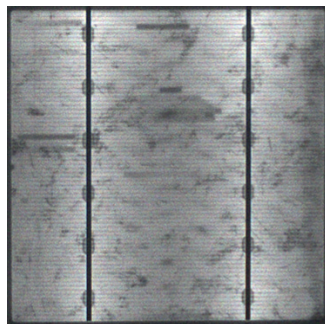


Fig. 4. Vertical current and voltage in a monocrystalline Si cell, along a finger crossed by two cracks: (a) unloaded and (b) loaded conditions.

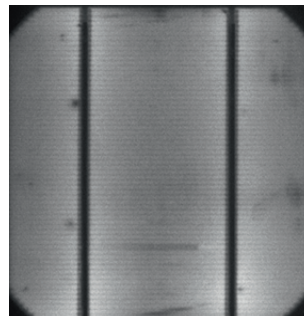
### 3. Electric model with spatially inhomogeneous series resistance

In polycrystalline Si cells, the local resistance,  $R_{loc}$ , is dishomogeneous and depends on grain boundaries and defects. This is clearly evidenced by a close analysis of a EL image, such that shown in Fig. 5a. The distribution of the brightness within the image does not depend only on the distance from the busbars as for monocrystalline Si (Fig. 5b), but several darker spots, representing grain boundaries and defects, are randomly distributed within the cell. In this case, the proposed model can be applied by introducing a spatially inhomogeneous series resistance instead of the homogeneous  $R_{loc}$ . Such a resistance can be defined as  $R_{ave}+dR$ , where  $R_{ave}$  is the average value and  $dR$  takes into account the fluctuations/perturbations using pseudo-random values taken from a Gaussian distribution with a prescribed variance.

The model has been applied along a grid line of an intact and a cracked polycrystalline cell, and the obtained vertical current densities are shown in Figs. 6a and 6b, respectively, compared to the experimental data. In particular, both the  $I_v$  distributions obtained by considering only  $R_{ave}$  and  $R_{ave}+dR$  are shown. A good matching with experimental data is obtained by assuming an amplitude of the perturbative term,  $dR$ , of about 30% the average value,  $R_{ave}$ .



(a) Polycrystalline Si cell



(b) Monocrystalline Si cell

Fig. 5. Electroluminescence images of intact mono- and polycrystalline Si cells.

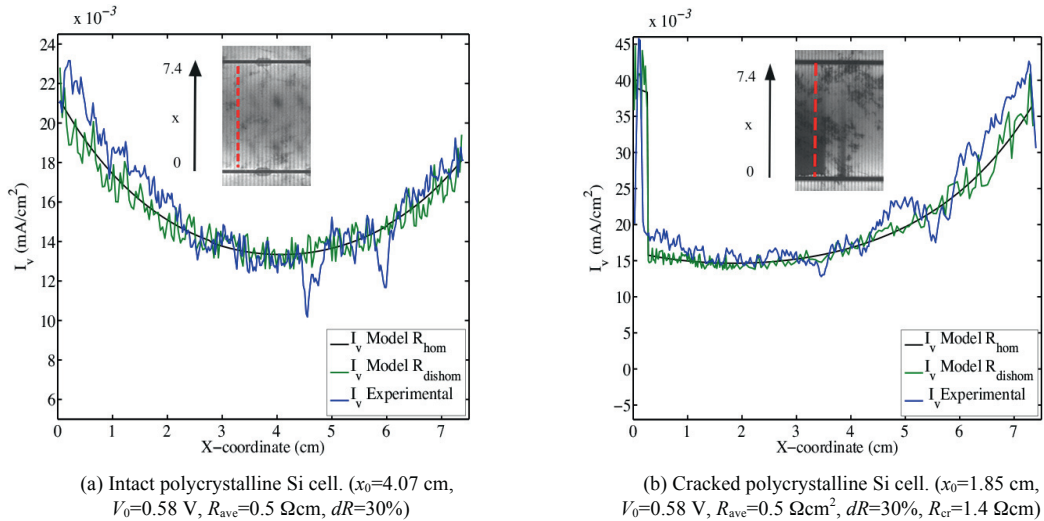


Fig. 6. Vertical current along a finger in a (a) intact and (b) cracked polycrystalline Si cell.

#### 4. Conclusions

In the present study, the one-dimensional model for current distribution in [11] has been generalized to the presence of cracks. The proposed method can be used to interpret the relation between voltage discontinuity and crack opening displacement at crack faces, correlating the crack opening, predicted according to nonlinear computational fracture mechanics simulations, and the localized resistance induced by the crack. In monocrystalline Si cells, the influence of crack opening on the electric response is evident, since the value of  $R_{cr}$  significantly increases by bending the module (see Figs. 3,4). In case of polycrystalline silicon, the scenario is much more complex due to a vertical current fluctuation caused by the contemporary presence of defects, grain boundaries and imperfections. Therefore, the use of a stochastic approach to model the local series resistance should be taken into account, as herein proposed.

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